
Machine Learning

Kernel Engineering

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Kernel Function Definition

Def. 2.26 *A kernel is a function k , such that $\forall \vec{x}, \vec{z} \in X$*

$$k(\vec{x}, \vec{z}) = \phi(\vec{x}) \cdot \phi(\vec{z})$$

where ϕ is a mapping from X to an (inner product) feature space.

- Kernel function are mappings such as

$$\vec{x} \in \mathfrak{R}^n, \quad \vec{\phi}(\vec{x}) = (\phi_1(\vec{x}), \phi_2(\vec{x}), \dots, \phi_m(\vec{x})) \in \mathfrak{R}^m$$



Valid Kernels

Def. B.11 *Eigen Values*

Given a matrix $\mathbf{A} \in \mathbb{R}^m \times \mathbb{R}^n$, an eigenvalue λ and an eigenvector $\vec{x} \in \mathbb{R}^n - \{\vec{0}\}$ are such that

$$\mathbf{A}\vec{x} = \lambda\vec{x}$$

Def. B.12 *Symmetric Matrix*

A square matrix $\mathbf{A} \in \mathbb{R}^n \times \mathbb{R}^n$ is symmetric iff $\mathbf{A}_{ij} = \mathbf{A}_{ji}$ for $i \neq j$ $i = 1, \dots, m$ and $j = 1, \dots, n$, i.e. iff $\mathbf{A} = \mathbf{A}'$.

Def. B.13 *Positive (Semi-) definite Matrix*

A square matrix $\mathbf{A} \in \mathbb{R}^n \times \mathbb{R}^n$ is said to be positive (semi-) definite if its eigenvalues are all positive (non-negative).



Valid Kernels cont'd

Proposition 2.27 (*Mercer's conditions*)

Let X be a finite input space with $K(\vec{x}, \vec{z})$ a symmetric function on X . Then $K(\vec{x}, \vec{z})$ is a kernel function if and only if the matrix

$$k(\vec{x}, \vec{z}) = \phi(\vec{x}) \cdot \phi(\vec{z})$$

is positive semi-definite (has non-negative eigenvalues).

- If the matrix is positive semi-definite then we can find a mapping ϕ implementing the kernel function



Valid Kernel operations

- $k(x,z) = k_1(x,z) + k_2(x,z)$
- $k(x,z) = k_1(x,z) * k_2(x,z)$
- $k(x,z) = \alpha k_1(x,z)$
- $k(x,z) = f(x)f(z)$
- $k(x,z) = k_1(\phi(x), \phi(z))$
- $k(x,z) = x'Bz$



Basic Kernels for unstructured data

- Linear Kernel
 - Your features
- Polynomial Kernel
 - Feature conjunctions
- Lexical kernel
 - similarity between your features



Kernels for structured data

- String Kernel
 - Character sequences
 - Word sequences
 - Spectrum kernel
- Tree kernels
 - Subtree,
 - Subset Tree,
 - Partial Tree kernels
 - Applies properties of string kernels



Kernel Engineering for Language Applications

- Basic Combinations
- *Canonical Mappings*, e.g. object transformations
- *Merging of Kernels*



Kernel Combinations an example

K_p^3 polynomial kernel of flat features

K_{Tree} Tree kernel

■ Kernel Combinations:

$$K_{Tree+P} = \gamma \times K_{Tree} + K_p^3,$$

$$K_{Tree \times P} = K_{Tree} \times K_p^3$$

$$K_{Tree+P} = \gamma \times \frac{K_{Tree}}{|K_{Tree}|} + \frac{K_p^3}{|K_p^3|},$$

$$K_{Tree \times P} = \frac{K_{Tree} \times K_p^3}{|K_{Tree}| \times |K_p^3|}$$



Object Transformation [CLJ 2008]

- $K(O_1, O_2) = \phi(O_1) \cdot \phi(O_2) = \phi_E(\phi_M(O_1)) \cdot \phi_E(\phi_M(O_2))$
 $= \phi_E(S_1) \cdot \phi_E(S_2) = K_E(S_1, S_2)$
- **Canonical Mapping, $\phi_M()$**
 - object transformation,
 - e. g. a syntactic parse tree, into a verb subcategorization frame tree.
- **Feature Extraction, $\phi_E()$**
 - maps the canonical structure in all its fragments
 - different fragment spaces, e. g. ST, SST and PT.



Predicate Argument Classification

- In an event:
 - target words describe relation among different entities
 - the participants are often seen as predicate's arguments.
- Example:

Paul gives a talk in Rome



Predicate Argument Classification

- In an event:
 - target words describe relation among different entities
 - the participants are often seen as predicate's arguments.

- Example:

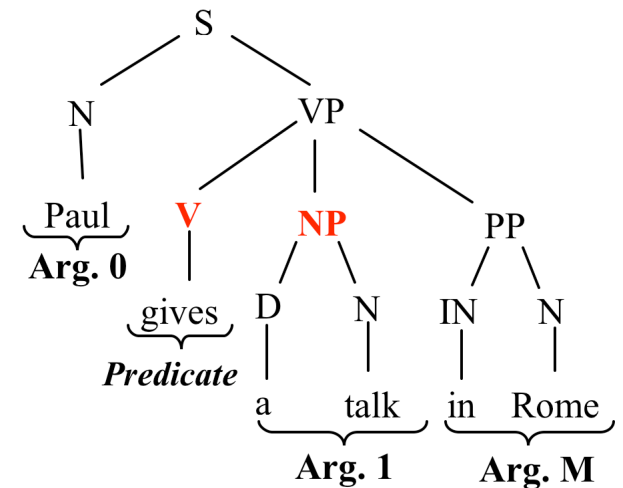
[*Arg0* Paul] [*predicate* gives] [*Arg1* a talk] [*ArgM* in Rome]



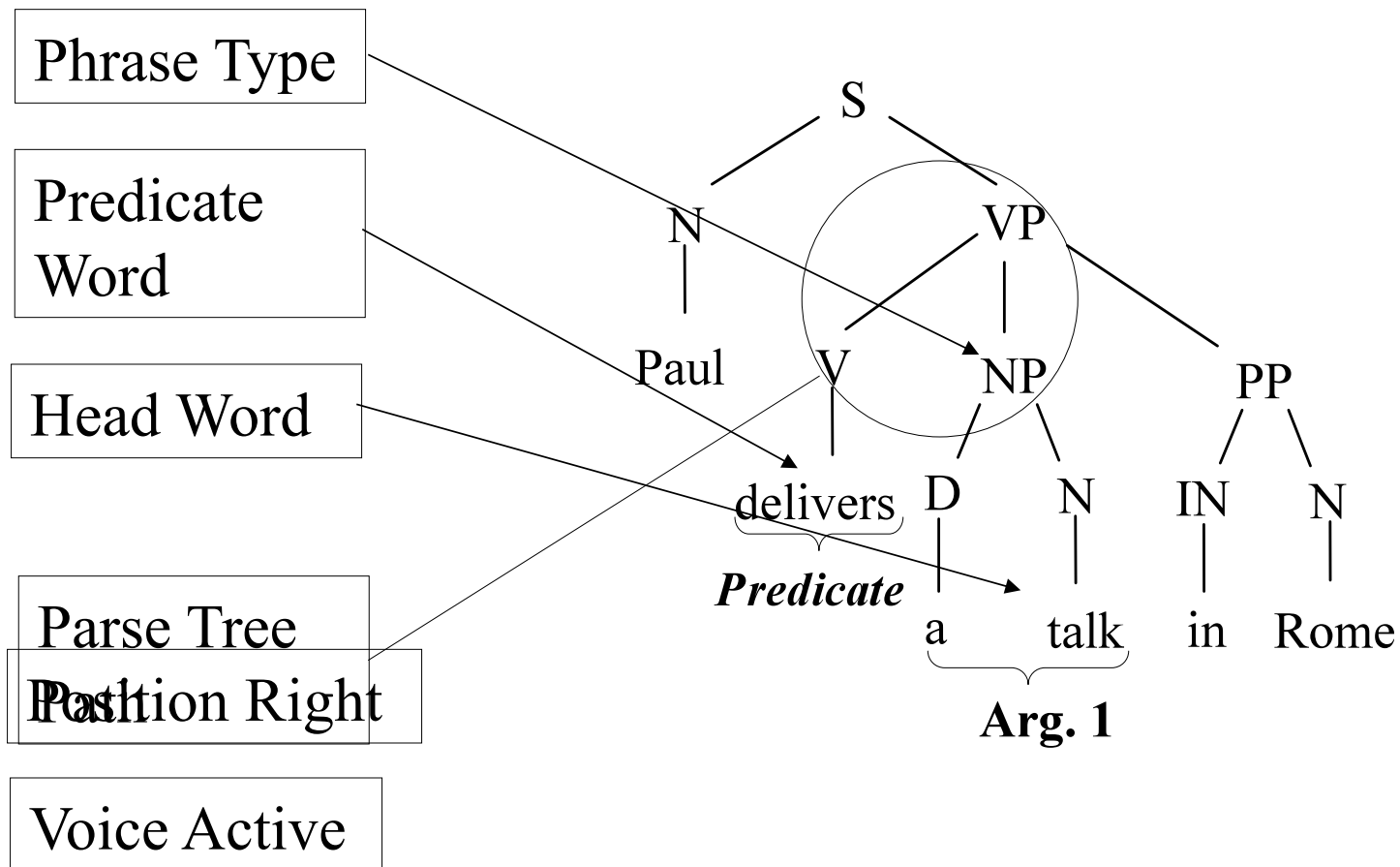
Predicate-Argument Feature Representation

Given a sentence, a predicate p :

1. Derive the sentence parse tree
2. For each node pair $\langle N_p, N_x \rangle$
 - a. Extract a feature representation set F
 - b. If N_x exactly covers the $Arg-i$, F is one of its positive examples
 - c. F is a negative example otherwise



Vector Representation for the linear kernel



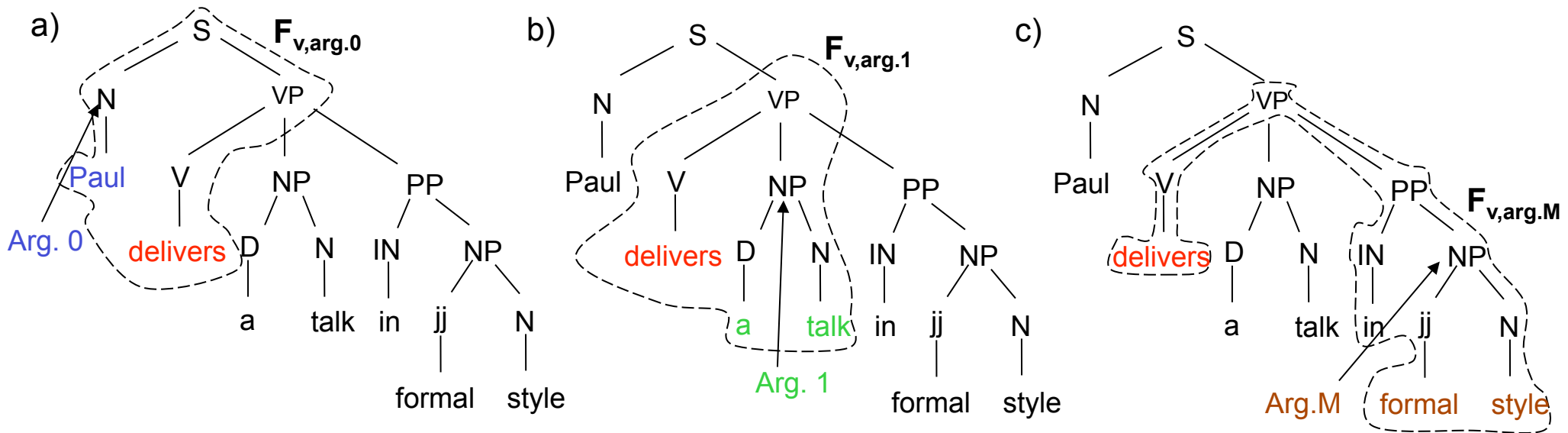
Kernel Engineering: Tree Tailoring



PAT Kernel [Moschitti, 2004]

- Given the sentence:

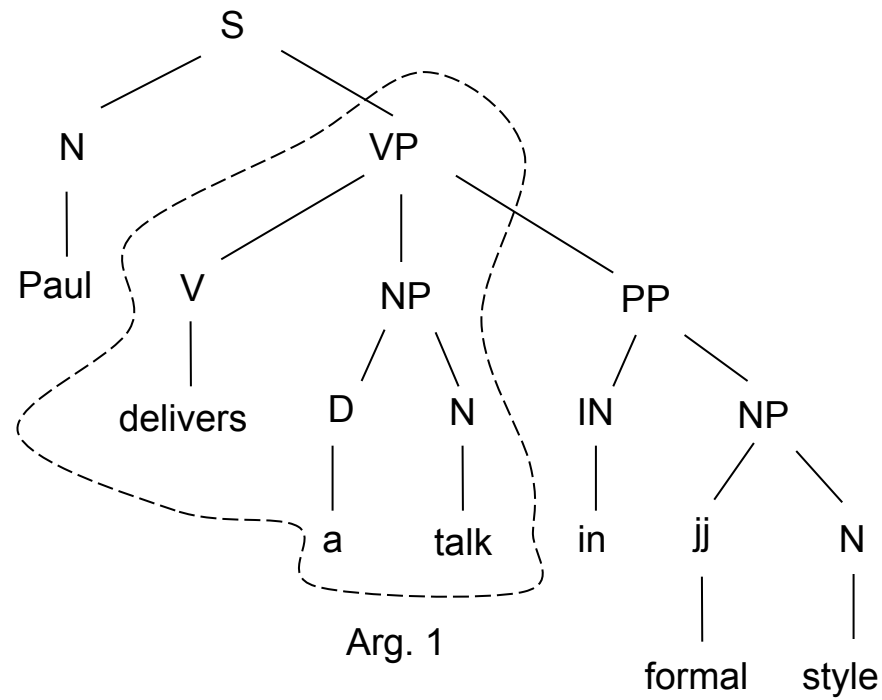
[*Arg0* Paul] [*predicate* delivers] [*Arg1* a talk] [*ArgM* in formal style]



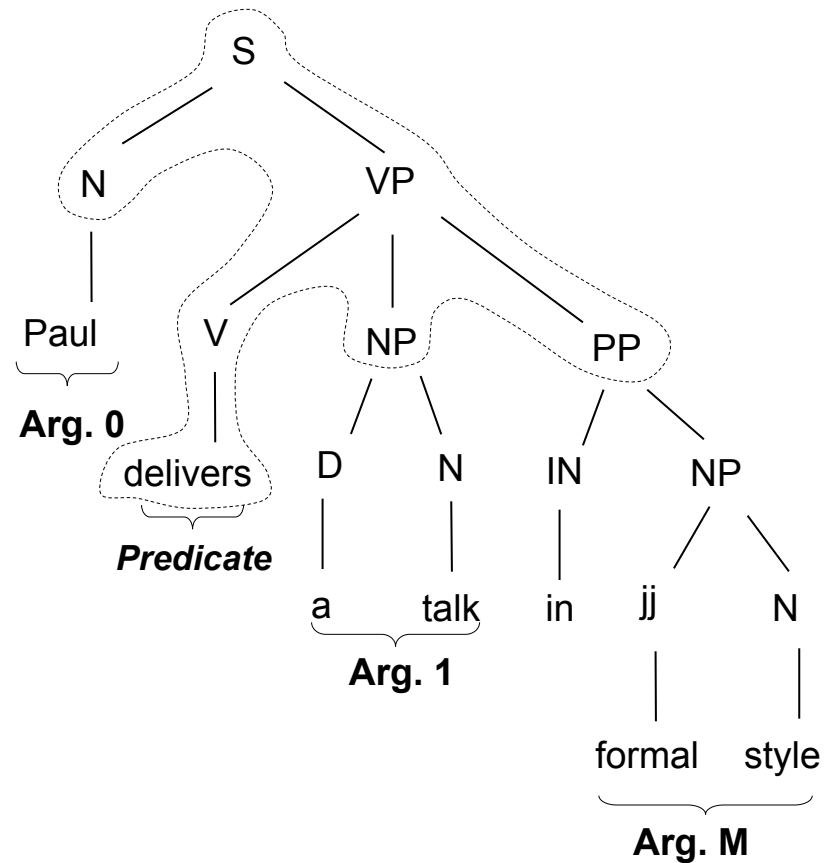
- These are Semantic Structures



In other words we consider...



Sub-Categorization Kernel (SCF) [Moschitti, 2004]

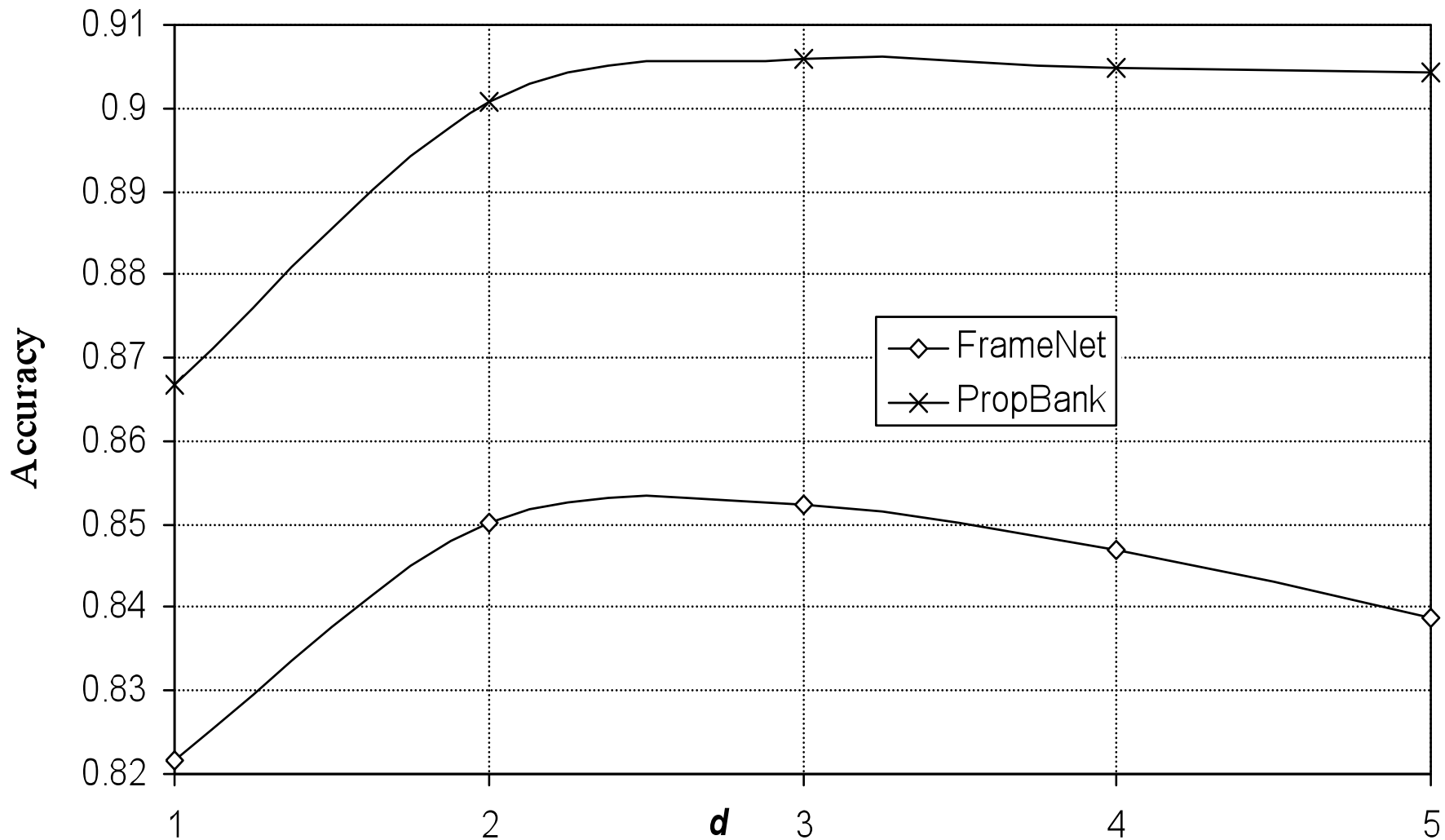


Experiments on Gold Standard Trees

- PropBank and PennTree bank
 - about 53,700 sentences
 - Sections from 2 to 21 train., 23 test., 1 and 22 dev.
 - Arguments from Arg0 to Arg5, ArgA and ArgM for a total of 122,774 and 7,359
- FrameNet and Collins' automatic trees
 - 24,558 sentences from the 40 frames of Senseval 3
 - 18 roles (same names are mapped together)
 - Only verbs
 - 70% for training and 30% for testing



Argument Classification with Poly Kernel

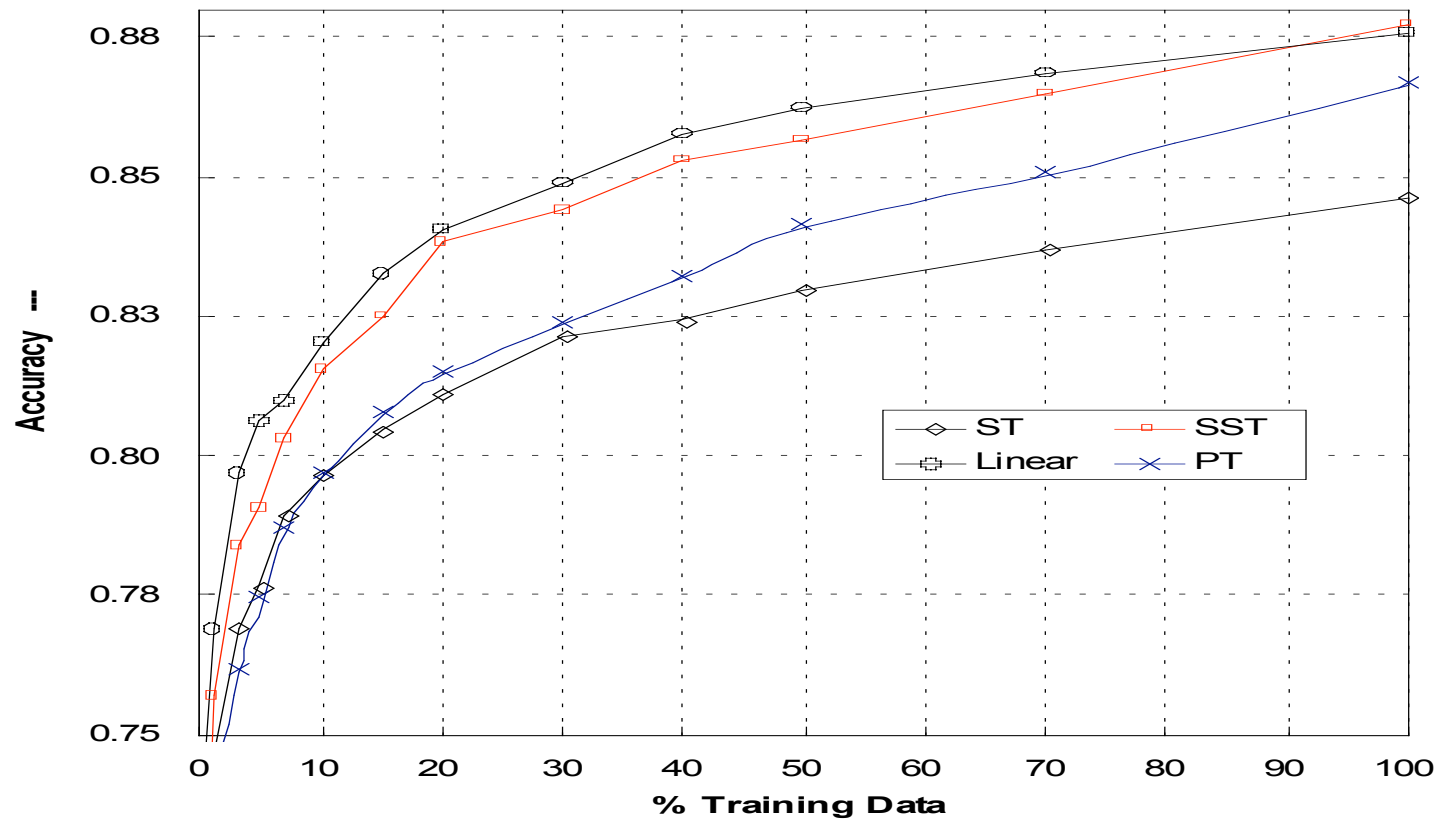


PropBank Results

Args	P3	PAT	PAT+P	PAT×P	SCF+P	SCF×P
Arg0	90.8	88.3	92.6	90.5	94.6	94.7
Arg1	91.1	87.4	91.9	91.2	92.9	94.1
Arg2	80.0	68.5	77.5	74.7	77.4	82.0
Arg3	57.9	56.5	55.6	49.7	56.2	56.4
Arg4	70.5	68.7	71.2	62.7	69.6	71.1
ArgM	95.4	94.1	96.2	96.2	96.1	96.3
Global Accuracy	90.5	88.7	91.3	90.4	92.4	93.2



Argument Classification on PAT using different Tree Fragment Extractor [Moschitti, ECML 2006]



FrameNet Results

Roles	P3	PAF	PAF+P	PAF×P	SCF+P	SCF×P
agent	92.0	88.5	91.7	91.3	93.1	93.9
cause	59.7	16.1	41.6	27.7	42.6	57.3
degree	74.9	68.6	71.4	57.8	68.5	60.9
depictive	52.6	29.7	51.0	28.6	46.8	37.6
duration	45.8	52.1	40.9	29.0	31.8	41.8
goal	85.9	78.6	85.3	82.8	84.0	85.3
instrument	67.9	46.8	62.8	55.8	59.6	64.1
manner	81.0	81.9	81.2	78.6	77.8	77.8
Global Acc. (18 roles)	85.2	79.5	84.6	81.6	83.8	84.2

- ProbBank arguments vs. Semantic Roles
-

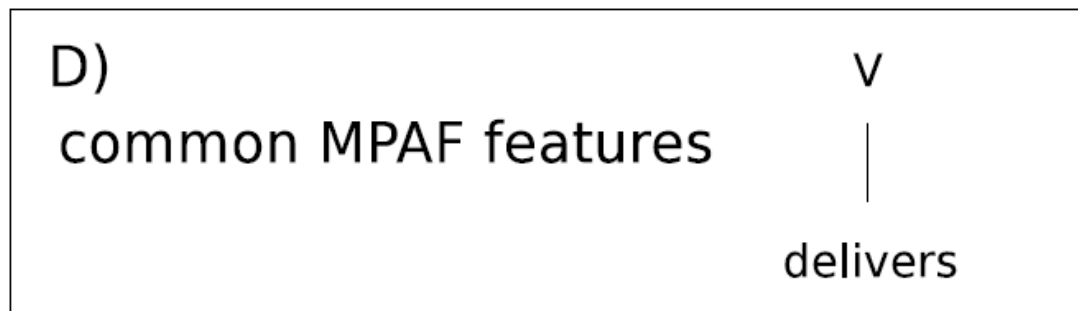
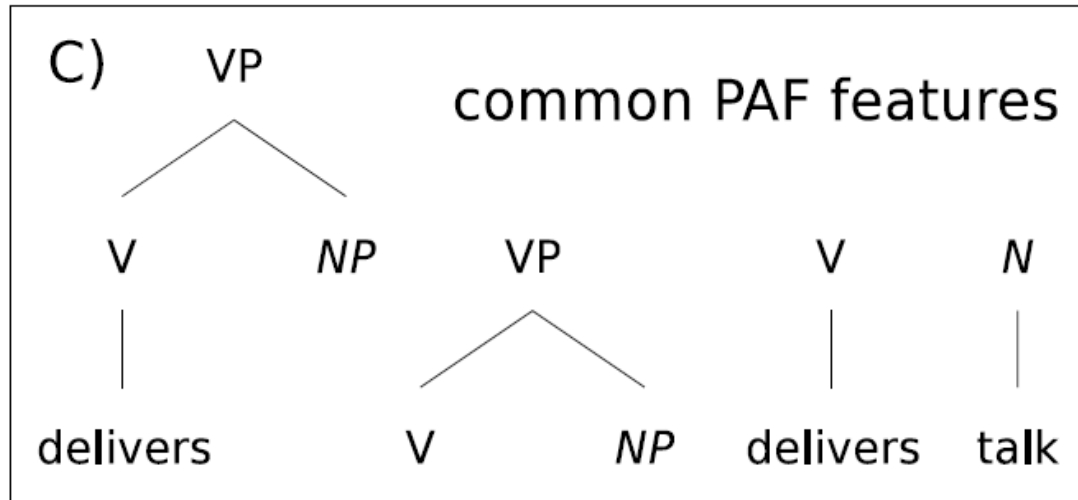


Kernel Engineering: Node marking

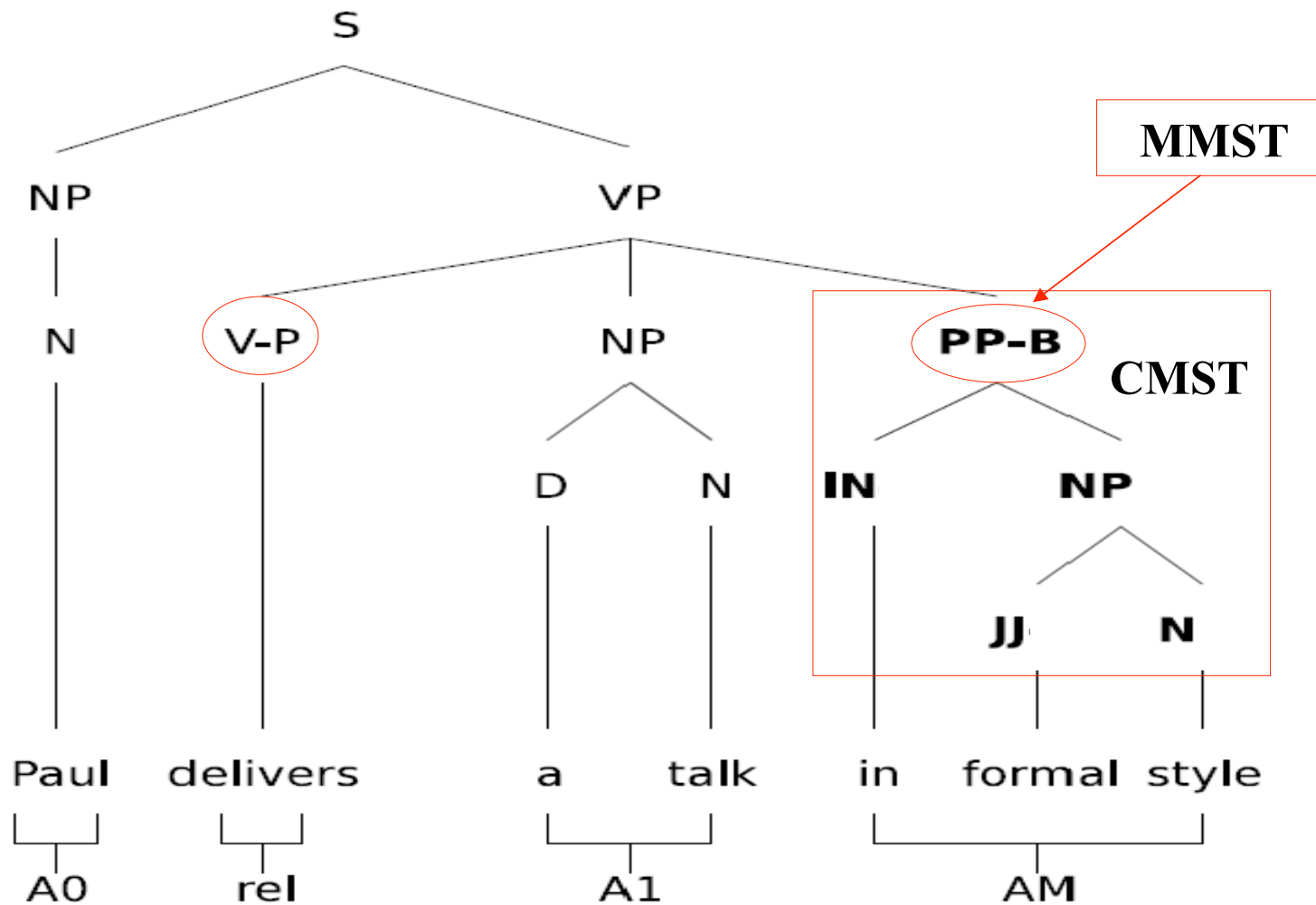
[Moschitti et al, CLJ 2008]



Node Marking Effect



Different tailoring and marking



Experiments

- PropBank and PennTree bank
 - about 53,700 sentences
 - Charniak trees from CoNLL 2005
- Boundary detection:
 - Section 2 training
 - Section 24 testing
 - PAF and MPAF



Number of examples/nodes of Section 2

Nodes	Section 2			Section 24		
	pos	neg	tot	pos	neg	tot
Internal	11,847	71,126	82,973	7,525	50,123	57,648
Pre-terminal	894	114,052	114,946	709	80,366	81,075
Both	12,741	185,178	197,919	8,234	130,489	138,723

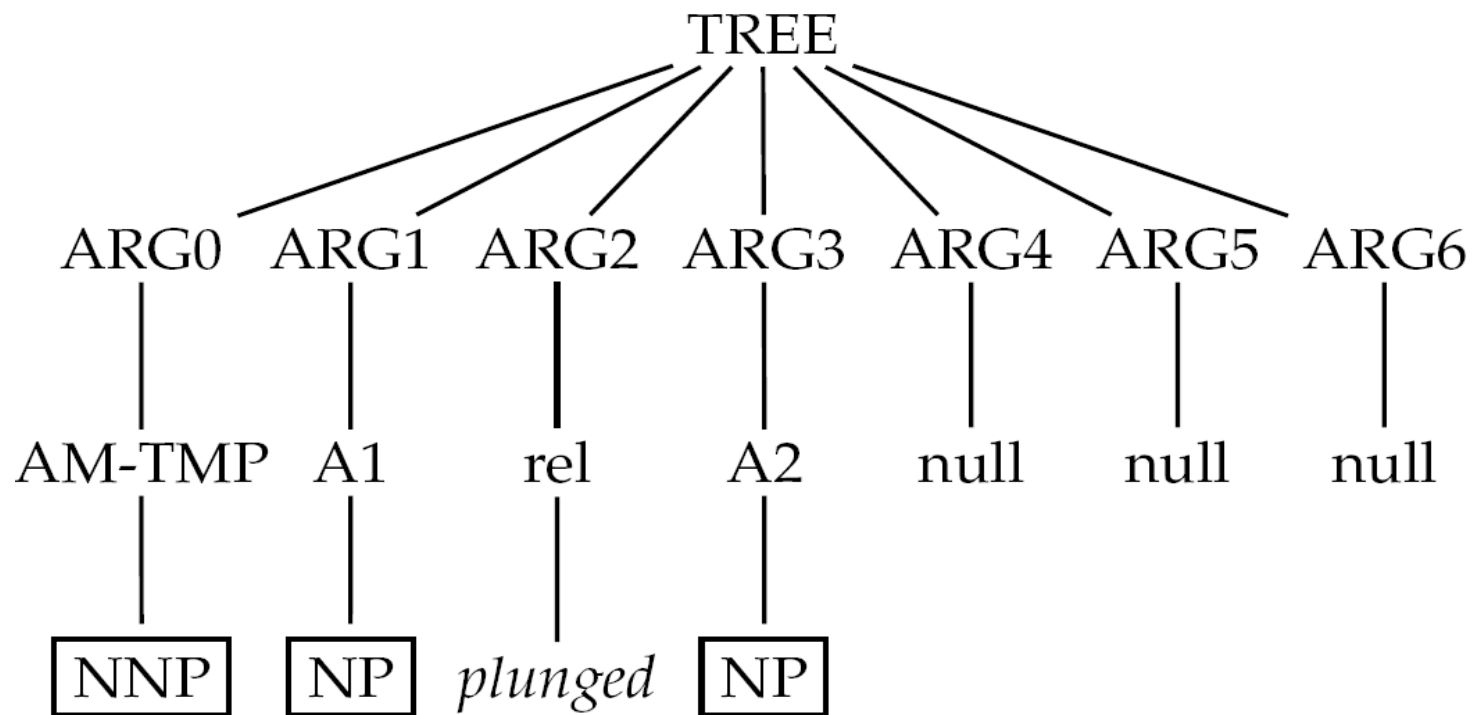


Predicate Argument Feature (PAF) vs. Marked PAF (MPAF) [ACL-ws-2005]

Tagging strategy	CPU _{time}	F1
PAF	5,179.18	75.24
MPAF	3,131.56	82.07



Other Canonical mappings: Semantic structures for re-ranking [Moschitti et al., CoNLL06]



Question Classification



Question Taxonomy

- **Definition:** What does HTML stand for?
- **Description:** What's the final line in the Edgar Allan Poe poem "The Raven"?
- **Entity:** What foods can cause allergic reaction in people?
- **Human:** Who won the Nobel Peace Prize in 1992?
- **Location:** Where is the Statue of Liberty?
- **Manner:** How did Bob Marley die?
- **Numeric:** When was Martin Luther King Jr. born?
- **Organization:** What company makes Bentley cars?

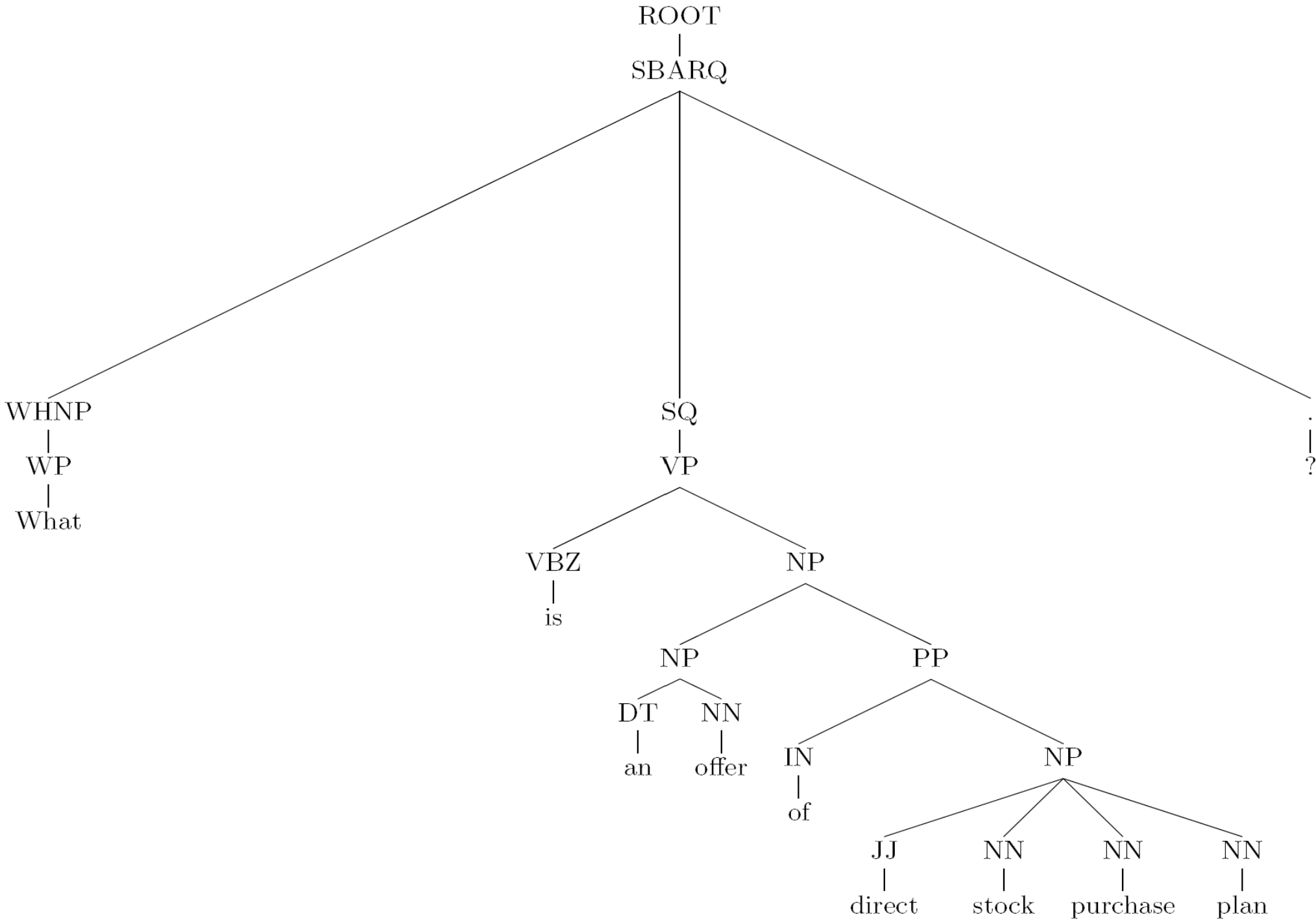


Question Classifier based on Tree Kernels

- Question dataset (<http://l2r.cs.uiuc.edu/~cogcomp/Data/QA/QC/>)
[Lin and Roth, 2005])
 - Distributed on 6 categories: Abbreviations, Descriptions, Entity, Human, Location, and Numeric.
- Fixed split 5500 training and 500 test questions
- Cross-validation (10-folds)
- Using the whole question parse trees
 - Constituent parsing
 - Example

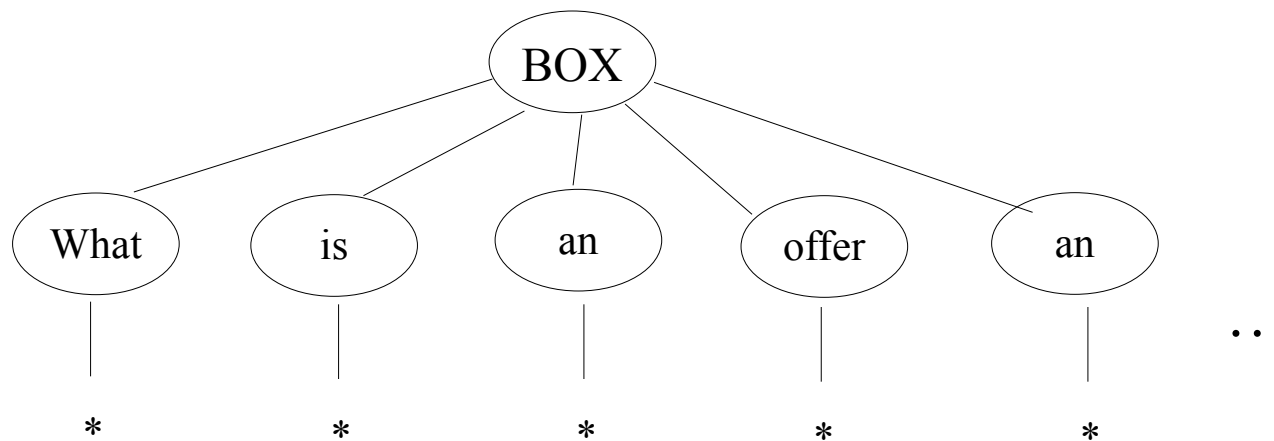
“What is an offer of direct stock purchase plan ?”





Kernels

- BOW, POS are obtained with a simple tree, e.g.



- PT (parse tree)
- PAS (predicate argument structure)



Question classification

Features	Accuracy (UIUC)	Accuracy (c.v.)
PT	90.4	84.8±1.4
BOW	90.6	84.7±1.4
PAS	34.2	43.0±2.2
POS	26.4	32.4±2.5
PT+BOW	91.8	86.1±1.3
PT+BOW+POS	91.8	84.7±1.7
PAS+BOW	90.0	82.1±1.5
PAS+BOW+POS	88.8	81.0±1.7



Merging of Kernels

[Bloehdorn and Moschitti, ECIR and CIKM 2007]:

- Syntactic/Semantic Tree Kernel
- Kernel Combinations
- Experiments



Efficient evaluation of the scalar product

$$\begin{aligned}\vec{x} \cdot \vec{z} &= \phi(T_x) \cdot \phi(T_z) = K(T_x, T_z) = \\ &= \sum_{n_x \in T_x} \sum_{n_z \in T_z} \Delta(n_x, n_z)\end{aligned}$$



Efficient evaluation of the scalar product

$$\begin{aligned}\vec{x} \cdot \vec{z} &= \phi(T_x) \cdot \phi(T_z) = K(T_x, T_z) = \\ &= \sum_{n_x \in T_x} \sum_{n_z \in T_z} \Delta(n_x, n_z)\end{aligned}$$

- [Collins and Duffy, ACL 2002] evaluate Δ in $O(n^2)$:

$\Delta(n_x, n_z) = 0$, if the productions are different else

$\Delta(n_x, n_z) = 1$, if pre - terminals else

$$\Delta(n_x, n_z) = \prod_{j=1}^{nc(n_x)} (1 + \Delta(ch(n_x, j), ch(n_z, j)))$$



Merging of Kernels

Definition 4 (Tree Fragment Similarity Kernel). For two tree fragments $f_1, f_2 \in \mathcal{F}$, we define the Tree Fragment Similarity Kernel as⁴:

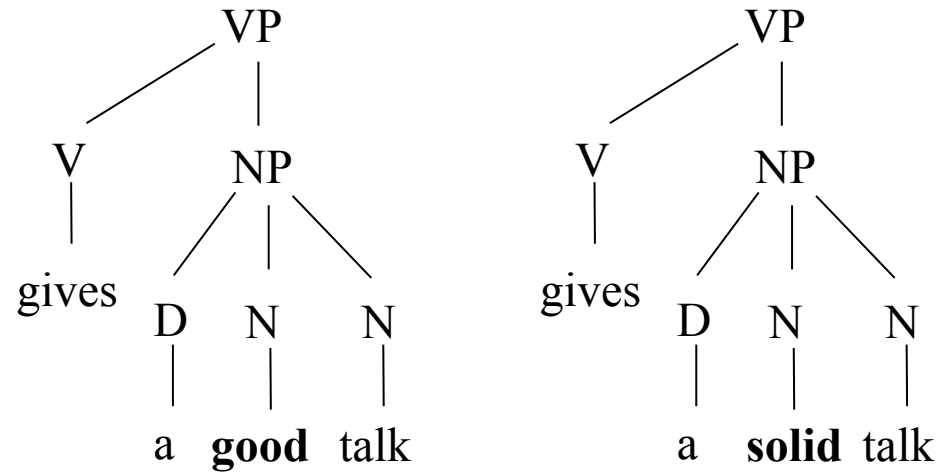
$$\kappa_{\mathcal{F}}(f_1, f_2) = \text{comp}(f_1, f_2) \prod_{t=1}^{nt(f_1)} \kappa_S(f_1(t), f_2(t))$$

$$\kappa_T(T_1, T_2) = \sum_{n_1 \in N_{T_1}} \sum_{n_2 \in N_{T_2}} \Delta(n_1, n_2)$$

where $\Delta(n_1, n_2) = \sum_{i=1}^{|\mathcal{F}|} \sum_{j=1}^{|\mathcal{F}|} I_i(n_1) I_j(n_2) \kappa_{\mathcal{F}}(f_i, f_j)$.



Merging of Kernels



$$\kappa_T(T_1, T_2) = \sum_{n_1 \in N_{T_1}} \sum_{n_2 \in N_{T_2}} \Delta(n_1, n_2)$$

where $\Delta(n_1, n_2) = \sum_{i=1}^{|\mathcal{F}|} \sum_{j=1}^{|\mathcal{F}|} I_i(n_1) I_j(n_2) \kappa_{\mathcal{F}}(f_i, f_j)$.



Delta Evaluation is very simple

0. if n_1 and n_2 are pre-terminals and $label(n_1) = label(n_2)$ then $\Delta(n_1, n_2) = \lambda \kappa_S(ch_{n_1}^1, ch_{n_2}^1)$,
1. if the productions at n_1 and n_2 are different then $\Delta(n_1, n_2) = 0$;
2. $\Delta(n_1, n_2) = \lambda$,
3. $\Delta(n_1, n_2) = \lambda \prod_{j=1}^{nc(n_1)} (1 + \Delta(ch_{n_1}^j, ch_{n_2}^j))$.



Similarity based on WordNet

Inverted Path Length:

$$sim_{IPL}(c_1, c_2) = \frac{1}{(1 + d(c_1, c_2))^\alpha}$$

Wu & Palmer:

$$sim_{WUP}(c_1, c_2) = \frac{2 \operatorname{dep}(lso(c_1, c_2))}{d(c_1, lso(c_1, c_2)) + d(c_2, lso(c_1, c_2)) + 2 \operatorname{dep}(lso(c_1, c_2))}$$

Resnik:

$$sim_{RES}(c_1, c_2) = -\log P(lso(c_1, c_2))$$

Lin:

$$sim_{LIN}(c_1, c_2) = \frac{2 \log P(lso(c_1, c_2))}{\log P(c_1) + \log P(c_2)}$$



Question Classification with S/STK

	Accuracy				
λ parameter	0.4	0.05	0.01	0.005	0.001
linear (bow)	0.905				
string matching	0.890	0.910	0.914	0.914	0.912
full	0.904	0.924	0.918	0.922	0.920
full-ic	0.908	0.922	0.916	0.918	0.918
path-1	0.906	0.918	0.912	0.918	0.916
path-2	0.896	0.914	0.914	0.916	0.916
lin	0.908	0.924	0.918	0.922	0.922
wup	0.908	0.926	0.918	0.922	0.922



Practical Example



SVM-light-TK Software

- Encodes ST, SST and combination kernels in SVM-light [Joachims, 1999]
- Available at <http://dit.unitn.it/~moschitt/>
- Tree forests, vector sets
- New extensions: the PT kernel will be released asap



Data Format

- “What does Html stand for?”

- 1 |BT| (SBARQ (WHNP (WP What))(SQ (AUX does))(NP (NNP S.O.S.))(VP (VB stand)(PP (IN for))))(. ?))

|BT| (**BOW** (What *) (does *) (S.O.S. *) (stand *) (for *) (? *))

|BT| (**BOP** (WP *) (AUX *) (NNP *) (VB *) (IN *) (. *))

|BT| (**PAS** (ARG0 (R-A1 (What *))) (ARG1 (A1 (S.O.S. NNP))) (ARG2 (rel stand)))

|ET| 1:1 21:2.742439465642236E-4 23:1 30:1 36:1 39:1 41:1 46:1 49:1
66:1 152:1 274:1 333:1

|BV| 2:1 21:1.4421347148614654E-4 23:1 31:1 36:1 39:1 41:1 46:1 49:1
52:1 66:1 152:1 246:1 333:1 392:1 |EV|



Basic Commands

- Training and classification
 - `./svm_learn -t 5 -C T train.dat model`
 - `./svm_classify test.dat model`
- Learning with a vector sequence
 - `./svm_learn -t 5 -C V train.dat model`
- Learning with the sum of vector and kernel sequences
 - `./svm_learn -t 5 -C + train.dat model`



Question and Answer Classification

Canonical Mapping + Kernel

Combinations



TASK: Automatic Classification

[Moschitti, CIKM 2008]

- The classifier detects if a pair (question and answer) is correct or not
- A representation for the pair is needed
- The classifier can be used to re-rank the output of a basic QA system



Dataset 2: TREC data

- 138 TREC 2001 test questions labeled as “description”
- 2,256 sentences, extracted from the best ranked paragraphs (using a basic QA system based on Lucene search engine on TREC dataset)
- 216 of which labeled as correct by one annotator



Dataset 2: TREC data

- 138 TREC 2001 test questions labeled as “description”

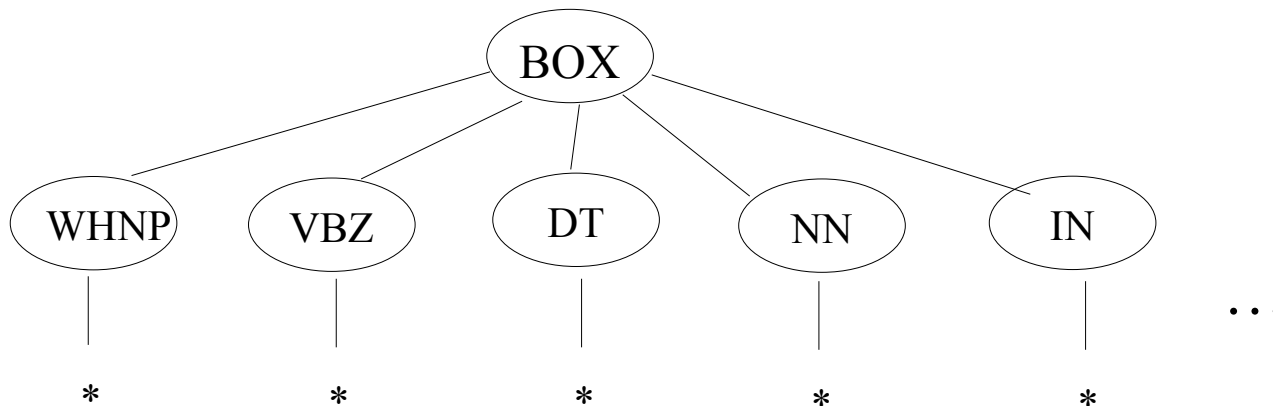
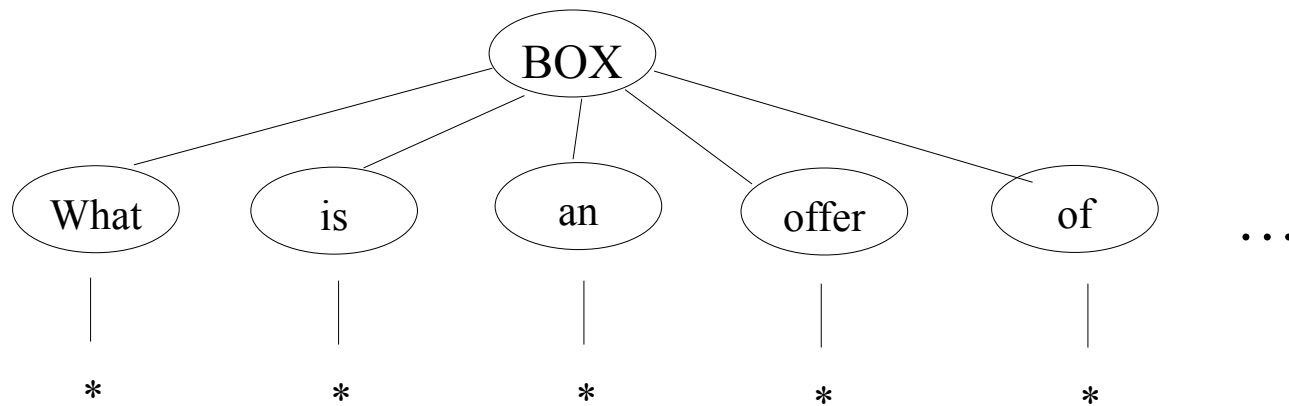
A question is linked to many answers: all its derived pairs cannot be shared by training and test sets

- 216 of which labeled as correct by one annotator



Bags of words (**BOW**) and POS-tags (**POS**)

- To save time, apply STK to these trees:



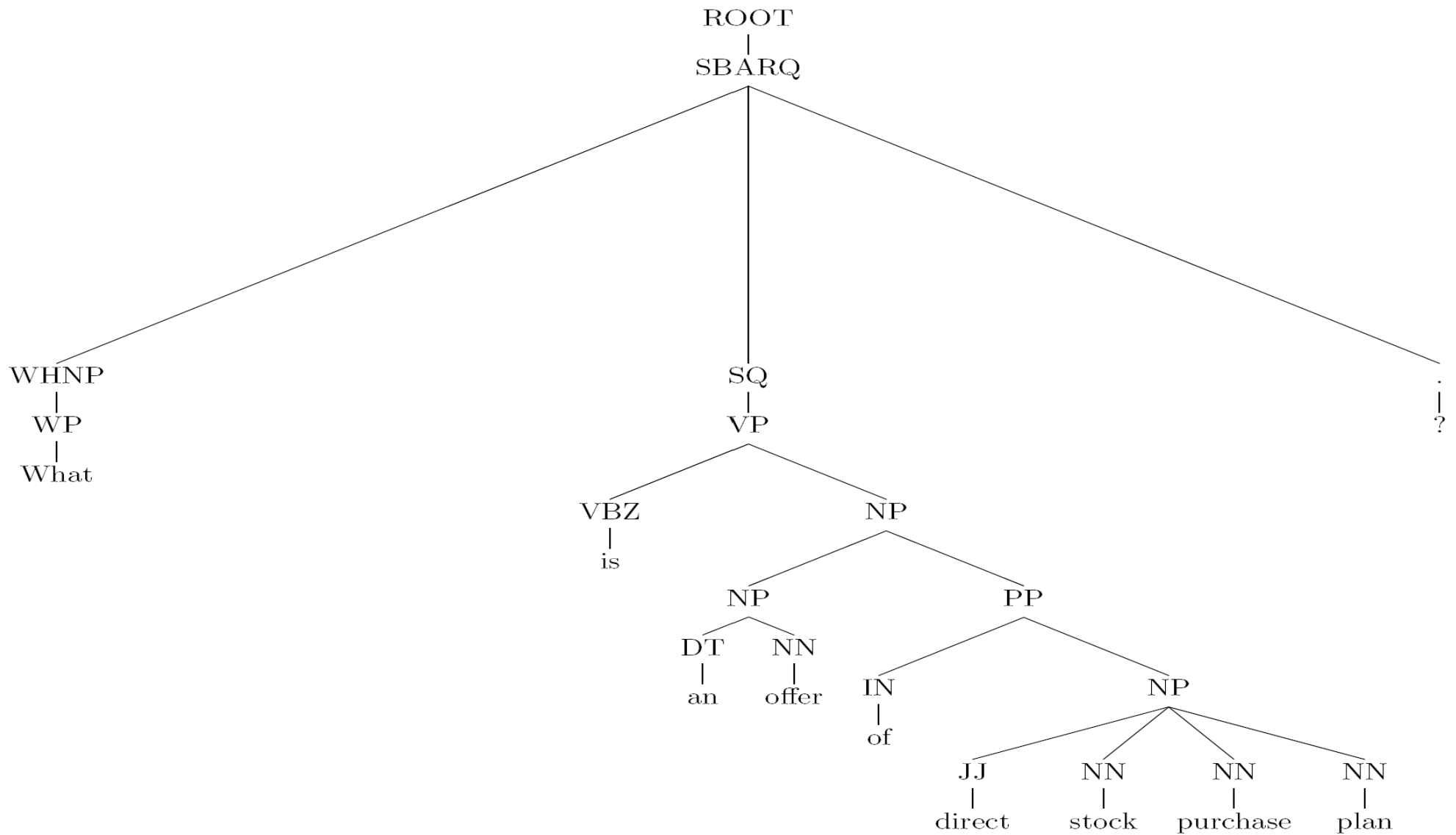
Word and POS Sequences

- What is an offer of...? (word sequence, **WSK**)
 - ➔ What_is_offer
 - ➔ What_is

- WHNP VBZ DT NN IN...(POS sequence, **POSSK**)
 - ➔ WHNP_VBZ_NN
 - ➔ WHNP_NN_IN



Syntactic Parse Trees (PT)



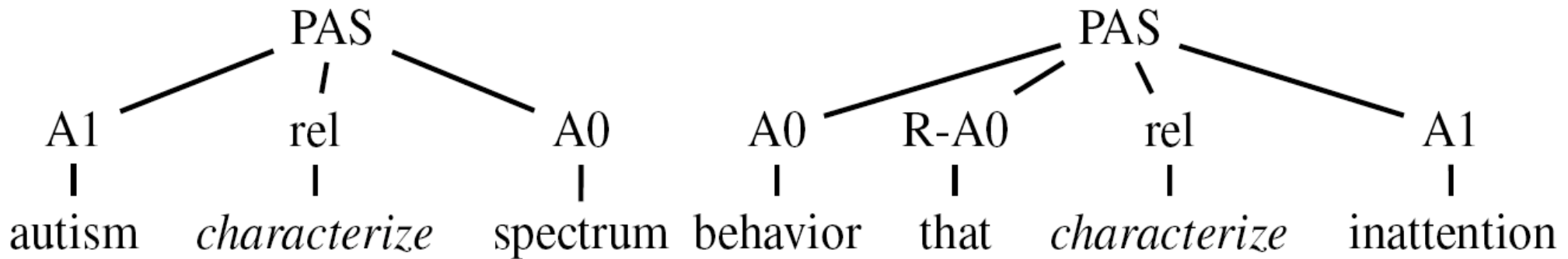
Predicate Argument Structure for Partial Tree Kernel (**PAS**_{PTK})

s₁: Autism is characterized by a broad spectrum of behavior that includes extreme inattention to surroundings and hypersensitivity to sound and other stimuli.,

[_{A1} Autism] is [_{rel} characterized] [_{A0} by a broad spectrum of behavior] [_{R-A0} that] [_{rel} includes] [_{A1} extreme inattention to surroundings and hypersensitivity to sound and other stimuli].



Predicate Argument Structure for Partial Tree Kernel (PAS_{PTK})



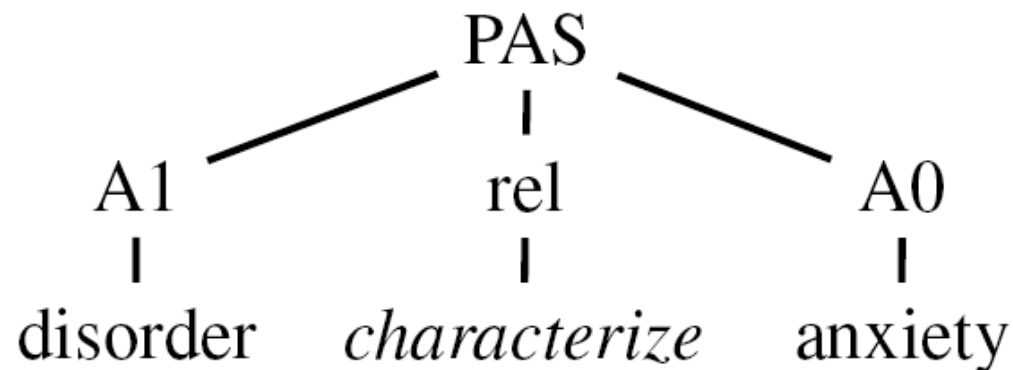
(a)



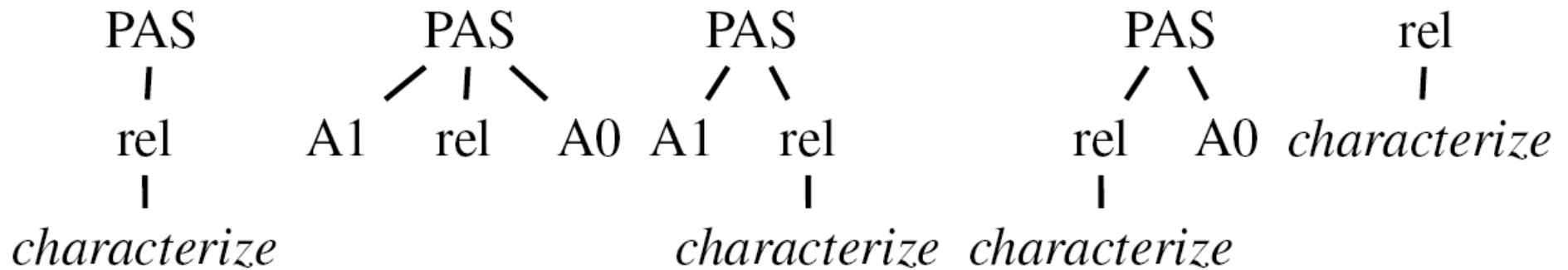
Predicate Argument Structure for Partial Tree Kernel (**PAS**_{PTK})

s₂: Panic disorder is characterized by unrealistic or excessive anxiety.

[_{A1} Panic disorder] is [_{rel} characterized] [_{A0} by unrealistic or excessive anxiety].



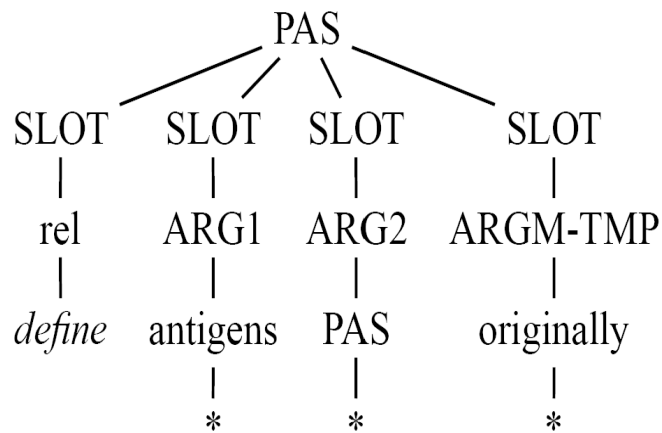
Common Substructures



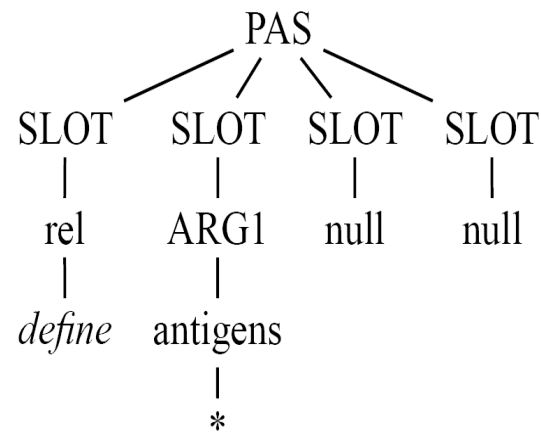
Shallow Semantic Trees for SST kernel

[Moschitti et al, ACL 2007]

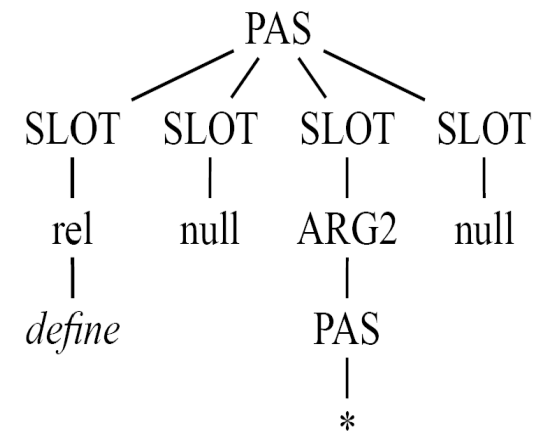
- To generate the substructures with STK we need to add slot nodes (from (a) obtain (b) and (c))



(a)



(b)



(c)

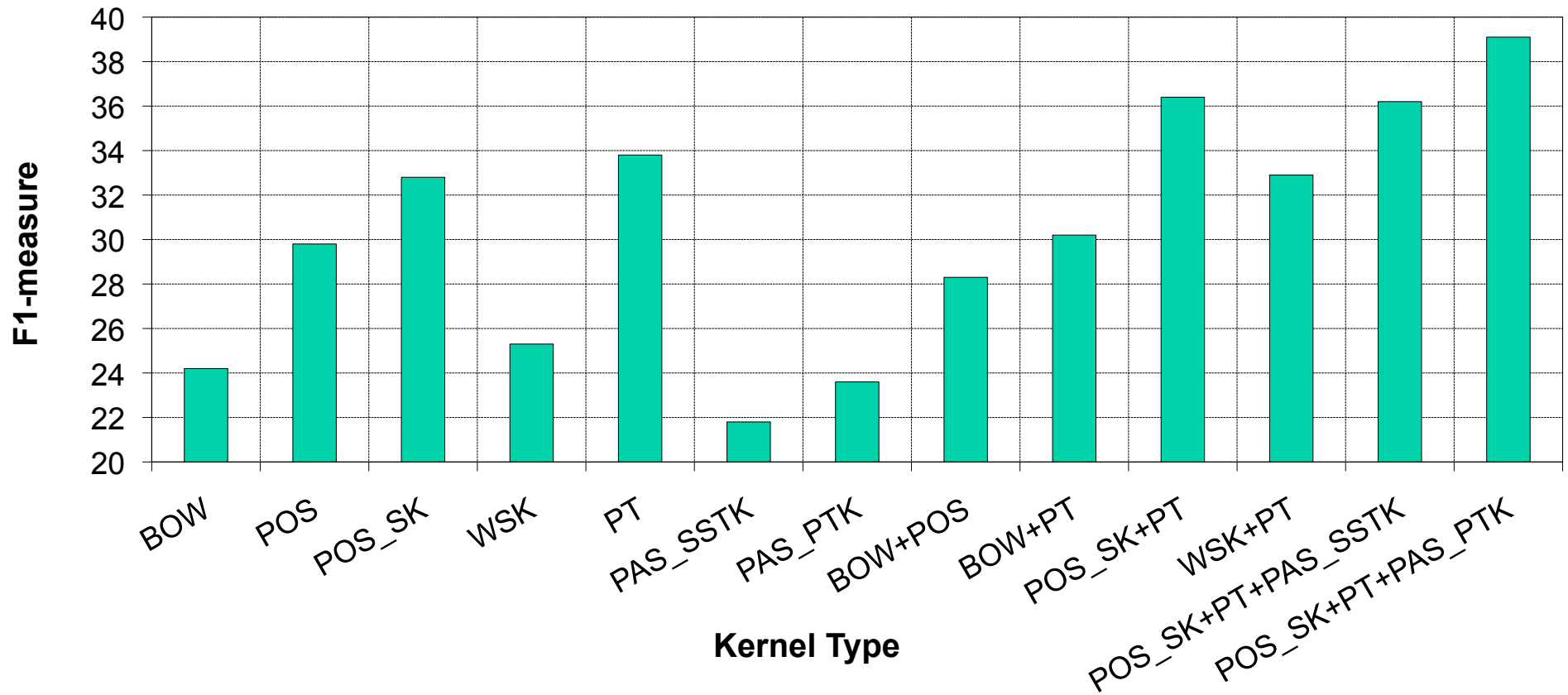


Kernels and Combinations

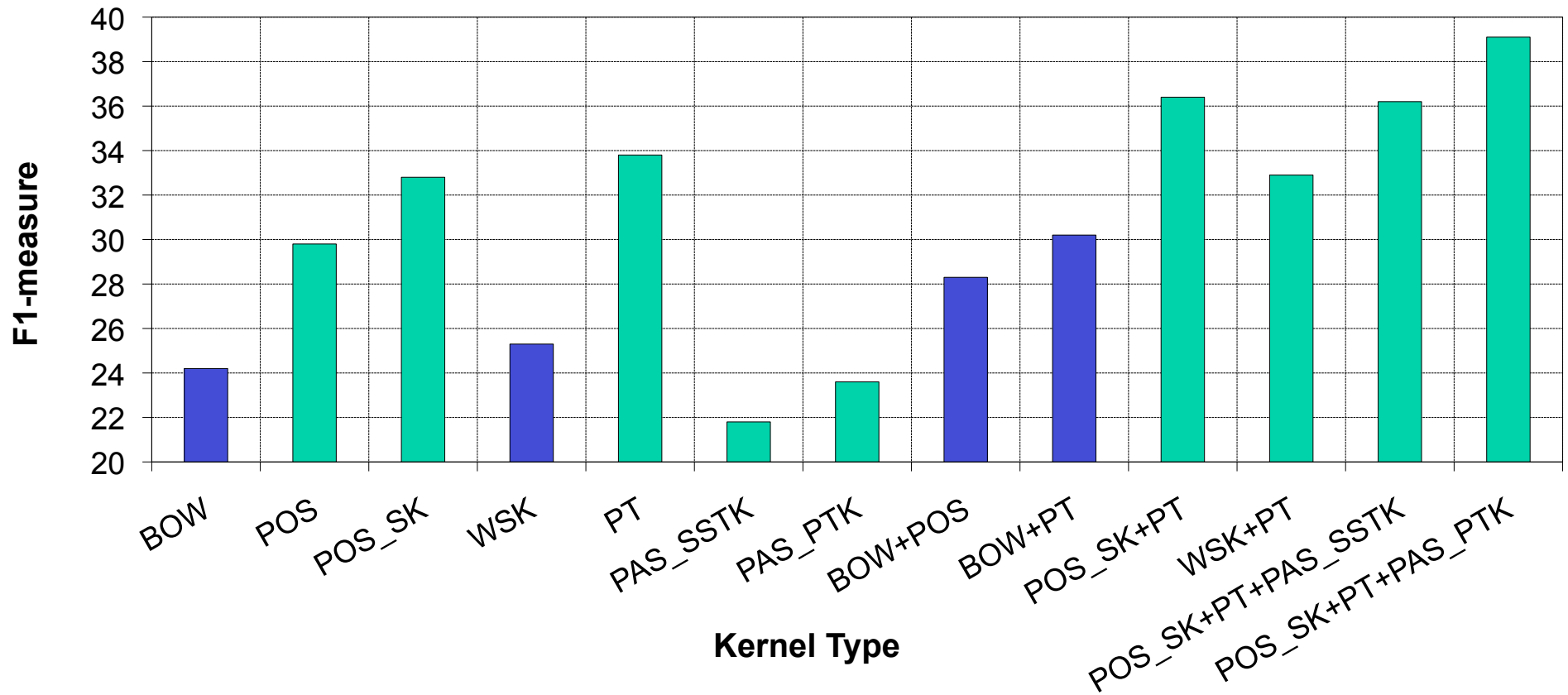
- Exploiting the property: $k(x,z) = k_1(x,z) + k_2(x,z)$
 - BOW, POS, WSK, POSSK, PT, PAS_{PTK}
- ⇒ BOW+POS, BOW+PT, PT+POS, ...



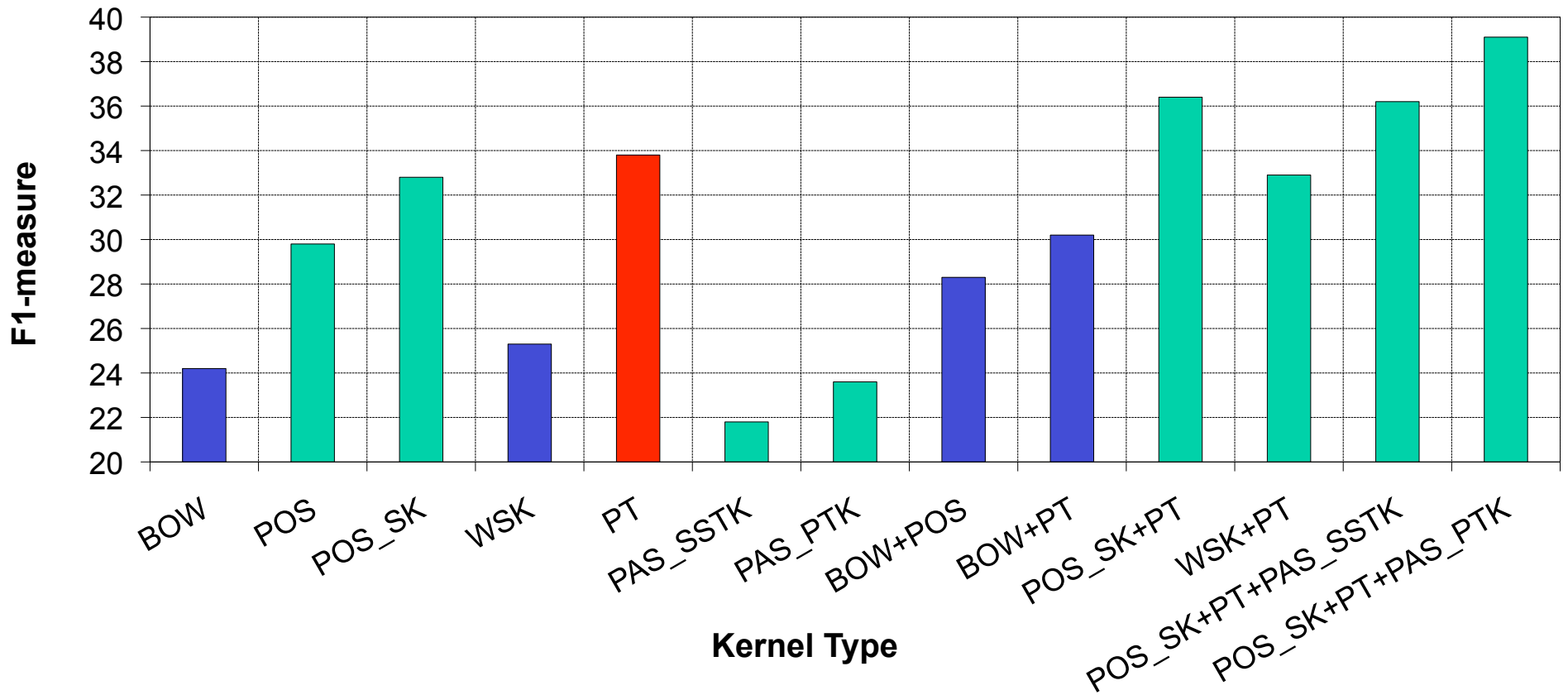
Results on TREC Data (5 folds cross validation)



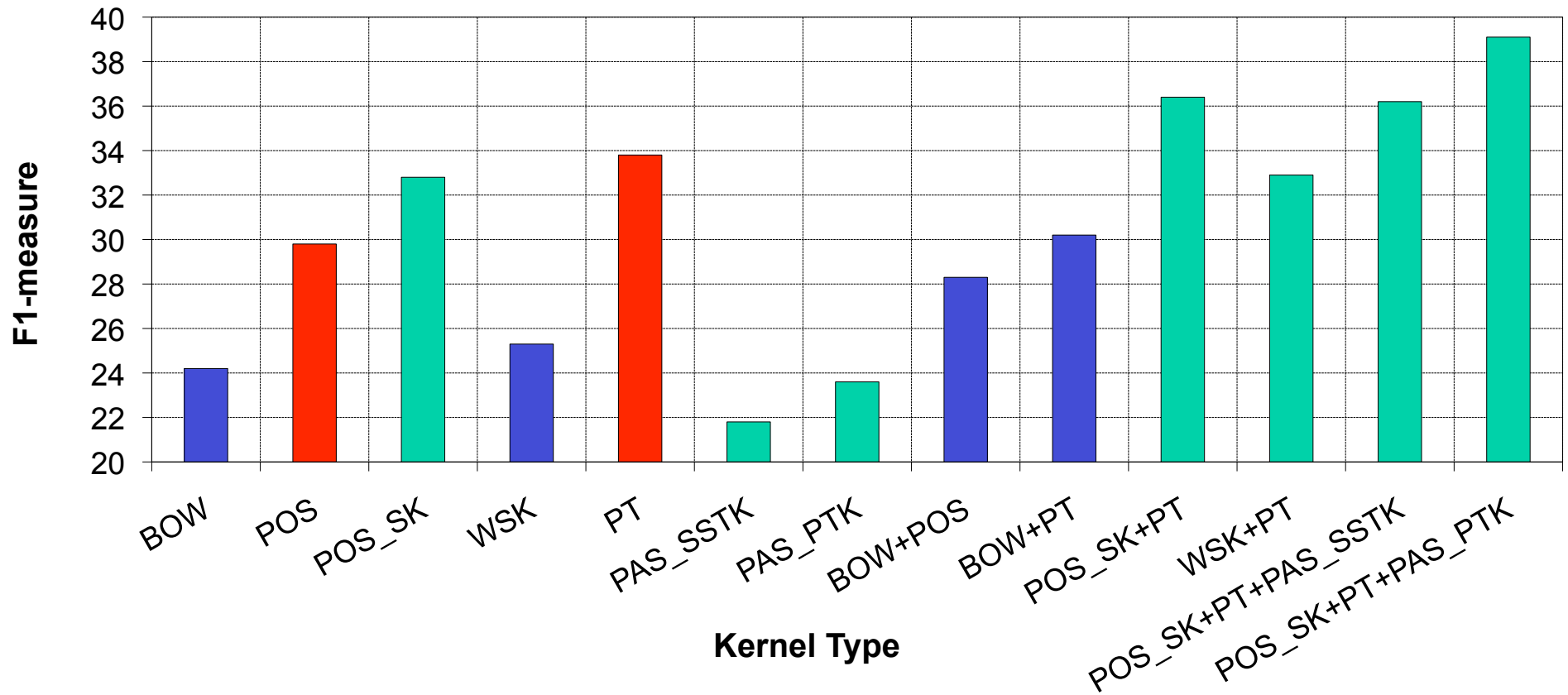
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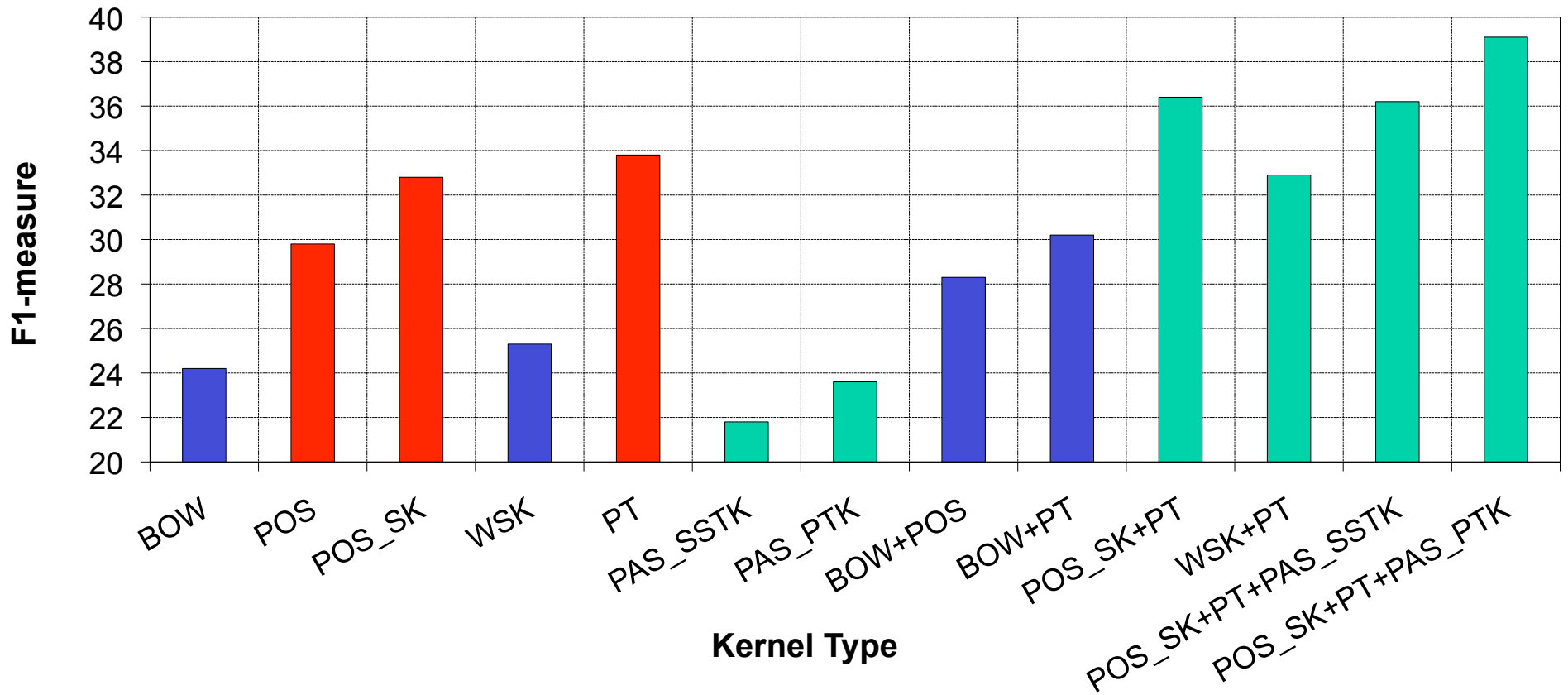
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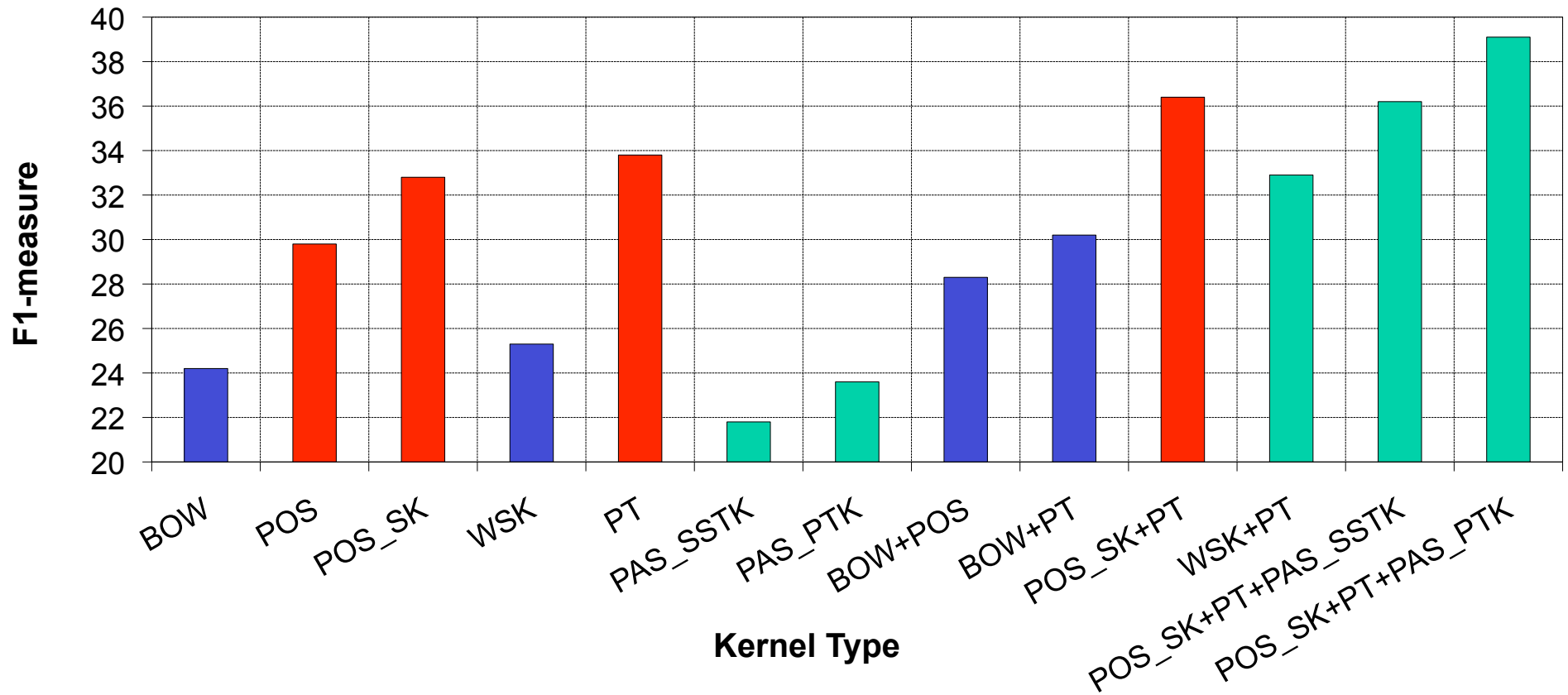
Results on TREC Data (5 folds cross validation)



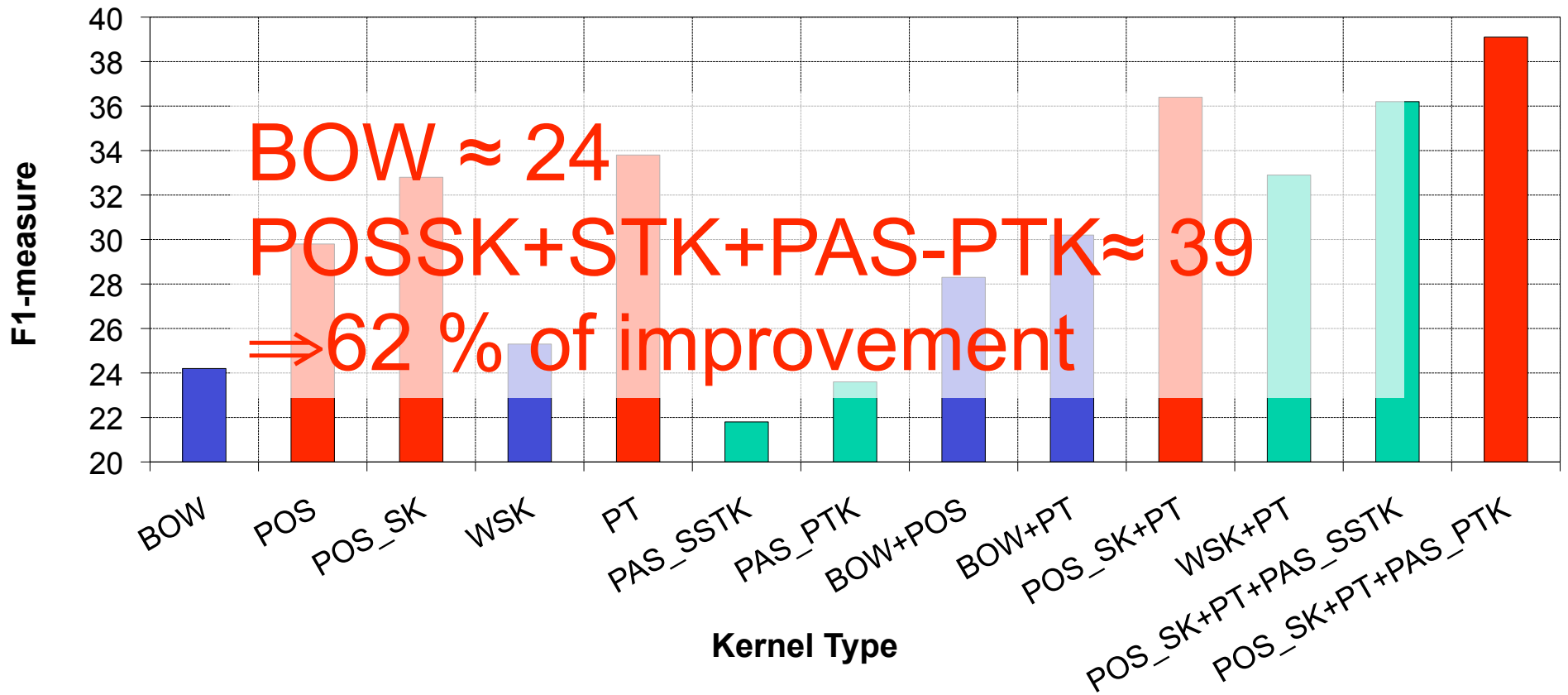
Results on TREC Data (5 folds cross validation)



Results on TREC Data (5 folds cross validation)



Results on TREC Data (5 folds cross validation)



Custom Kernel

- `double custom_kernel(KERNEL_PARM *kernel_parm, DOC *a, DOC *b) {`
- `int i=0; double k1;`
- `k1 = tree_kernel(kernel_parm, a, b, i, i);`
- `return k1;`
- `}`



Conclusions

- Kernel methods and SVMs are useful tools to design language applications
- Kernel design still require some level of expertise
- Engineering approaches to tree kernels
 - Basic Combinations
 - Canonical Mappings, e.g.
 - Node Marking
 - Merging of kernels in more complex kernels
- State-of-the-art in SRL and QC
- An efficient tool to use them



Thank you

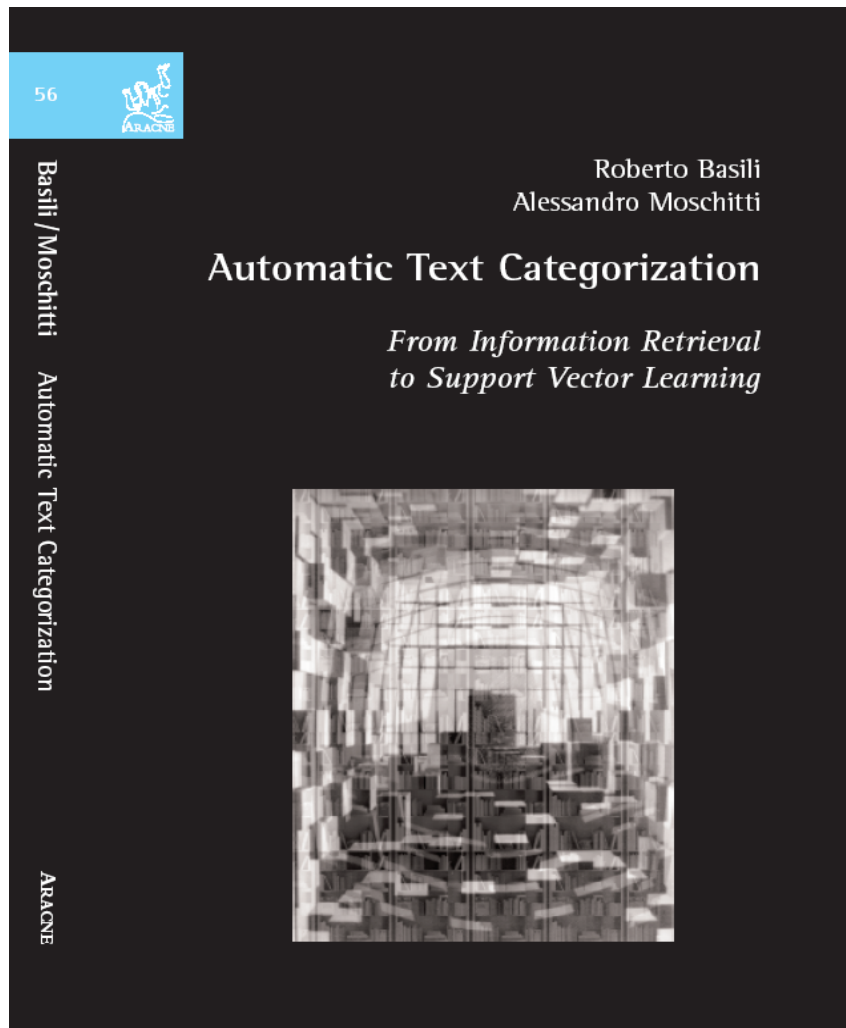


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An introductory book on SVMs, Kernel methods and Text Categorization



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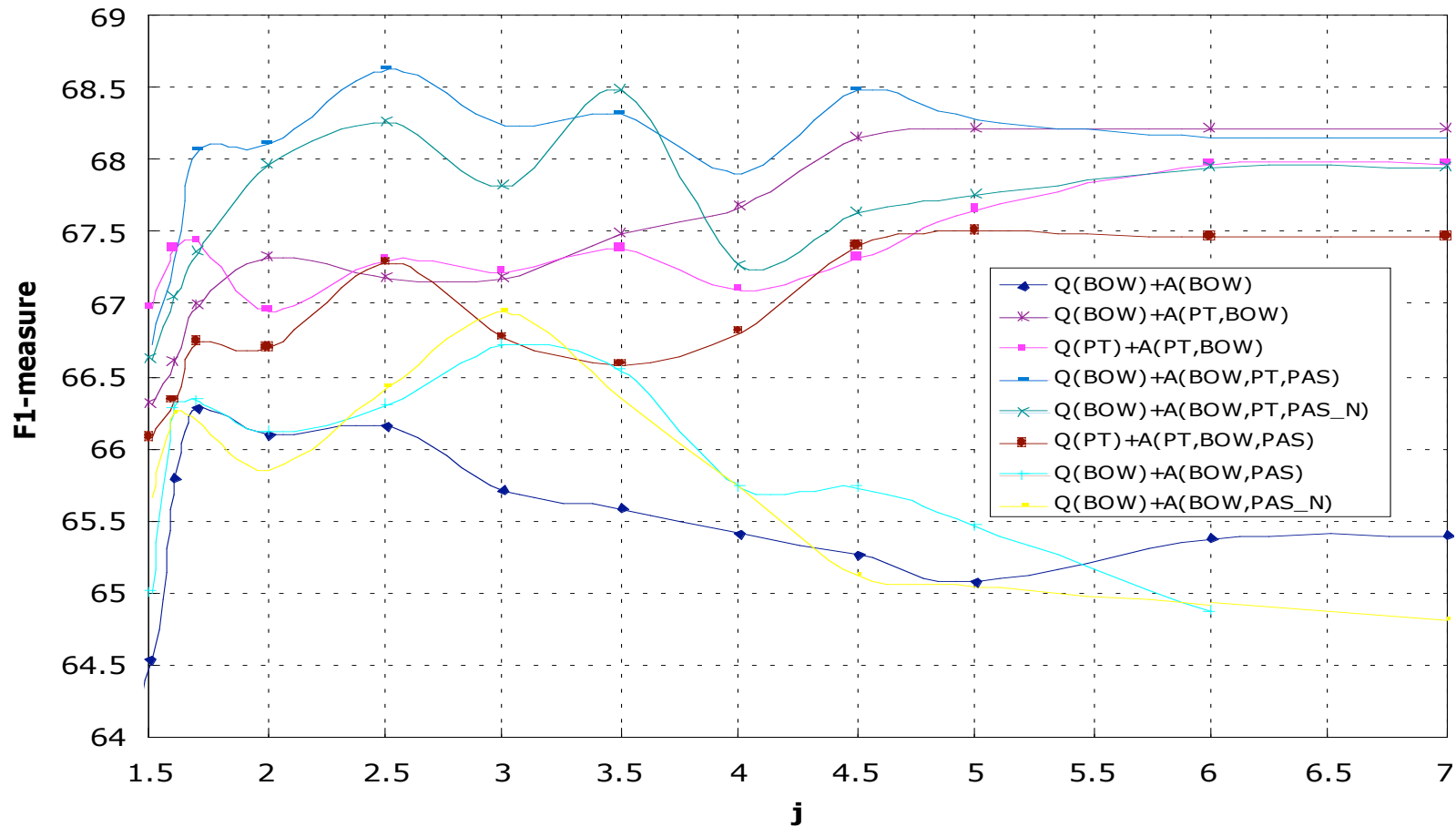


```

function Evaluate_Pair_Set(Tree  $T_1$ ,  $T_2$ ) returns NODE_PAIR_SET;
LIST  $L_1, L_2$ ;
NODE_PAIR_SET  $N_p$ ;
begin
   $L_1 = T_1$ .ordered_list;
   $L_2 = T_2$ .ordered_list; /*the lists were sorted at loading time*/
   $n_1 = \text{extract}(L_1)$ ; /*get the head element and*/
   $n_2 = \text{extract}(L_2)$ ; /*remove it from the list*/
  while ( $n_1$  and  $n_2$  are not NULL)
    if (production_of( $n_1$ ) > production_of( $n_2$ ))
      then  $n_2 = \text{extract}(L_2)$ ;
    else if (production_of( $n_1$ ) < production_of( $n_2$ ))
      then  $n_1 = \text{extract}(L_1)$ ;
    else
      while (production_of( $n_1$ ) == production_of( $n_2$ ))
        while (production_of( $n_1$ ) == production_of( $n_2$ ))
          add( $\langle n_1, n_2 \rangle$ ,  $N_p$ );
           $n_2 = \text{get\_next\_elem}(L_2)$ ; /*get the head element
          and move the pointer to the next element*/
        end
         $n_1 = \text{extract}(L_1)$ ;
        reset( $L_2$ ); /*set the pointer at the first element*/
      end
    end
  end
  return  $N_p$  ;
end

```

The Impact of SSTK in Answer Classification



Mercer's conditions (1)

Def. B.11 *Eigen Values*

Given a matrix $\mathbf{A} \in \mathbb{R}^m \times \mathbb{R}^n$, an eigenvalue λ and an eigenvector $\vec{x} \in \mathbb{R}^n - \{\vec{0}\}$ are such that

$$\mathbf{A}\vec{x} = \lambda\vec{x}$$

Def. B.12 *Symmetric Matrix*

A square matrix $\mathbf{A} \in \mathbb{R}^n \times \mathbb{R}^n$ is symmetric iff $\mathbf{A}_{ij} = \mathbf{A}_{ji}$ for $i \neq j$ $i = 1, \dots, m$ and $j = 1, \dots, n$, i.e. iff $\mathbf{A} = \mathbf{A}'$.

Def. B.13 *Positive (Semi-) definite Matrix*

A square matrix $\mathbf{A} \in \mathbb{R}^n \times \mathbb{R}^n$ is said to be positive (semi-) definite if its eigenvalues are all positive (non-negative).



Mercer's conditions (2)

Proposition 2.27 (*Mercer's conditions*)

Let X be a finite input space with $K(\vec{x}, \vec{z})$ a symmetric function on X . Then $K(\vec{x}, \vec{z})$ is a kernel function if and only if the matrix

$$k(\vec{x}, \vec{z}) = \phi(\vec{x}) \cdot \phi(\vec{z})$$

is positive semi-definite (has non-negative eigenvalues).

- If the Gram matrix: $G = k(\vec{x}_i, \vec{x}_j)$ is positive semi-definite there is a mapping ϕ that produces the target kernel function



The lexical semantic kernel is not always a kernel

- It may not be a kernel so we can use $M' \cdot M$, where M is the initial similarity matrix

Proposition B.14 *Let A be a symmetric matrix. Then A is positive (semi-)definite iff for any vector $\vec{x} \neq 0$*

$$\vec{x}' A \vec{x} > \lambda \vec{x}' \vec{x} \quad (\lambda \geq 0).$$

From the previous proposition it follows that: If we find a decomposition A in $M' M$, then A is semi-definite positive matrix as

$$\vec{x}' A \vec{x} = \vec{x}' M' M \vec{x} = (M \vec{x})' (M \vec{x}) = M \vec{x} \cdot M \vec{x} = \|M \vec{x}\|^2 \geq 0.$$

